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Efficient VLSI Implementation of Modified Dual Tree Discrete Wavelet Transform Based on Lifting Scheme

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ABSTRACT

In past few decades, dual tree discrete wavelet transform (DT-DWT) has become an open active research area for image processing applications. Nowadays; lifting based DT-DWT seeks more attention due to its lower computational complexity and shift invariance property. Nevertheless, VLSI implementation of lifting based DT-DWT further needs to be improved for low power and high speed image processing applications. In this article, an efficient VLSI implementation of modified lifting based DT-DWT is proposed. In proposed approach, two real valued lifting based filters are used to implement dual tree structure in which six high pass bands (i.e., two HH, two HL and two LH) and two low pass bands (LL) are obtained. Next, high frequency components (HH1 and HH2) as well as low pass bands (LL1 and LL2) are merged togetheras single sub bands HHm and LLm respectively. In synthesis section, the original image is recovered using LL_m, HH_m, and LH2and HL2 without considering the two high pass bands (HL1and LH1).Hence, the proposed approach greatly reduces the hardware requirements and consumes less power than the DT-DWT without affecting the image quality. Experiment was carried out and tested on various test images using Xilinx ISE and MATLAB R2010a. The experiment results inferred that the proposed approach is well suited for image compression.

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INTRODUCTION

In current years, discrete wavelet transform (DWT) is widely used for image processing applications because of its ability to represent the signal in different scale, highest energy compaction, multi resolution, and higher compression ratio. However, the realization of DWT demands higher computationally complexity and more memory storage which are not appropriate for high speed and low power image/video processing applications (Tinku Acharya and Chaitali Chakrabarti, 2006). Sweldens (1996) and Daubechies (1998) proposed a lifting based DWT which requires fewer arithmetic computations. In lifting-based DWT (LDWT) scheme, the wavelet filter matrix is divided into successive matrices including diagonal, upper triangular and lower triangular matrices. Then, the wavelet filters are implemented using banded matrices multiplications (Sweldens, 1996 and Daubechies, 1998). Several lifting based DWT architectures have been proposed for image processing applications. These architectures may include folded lifting based DWT (Andra *et al*., 2002), systolic array DWT (Huang *et al*., 2002), and recursive lifting based DWT (Xiong *et al*., 2006). Conversely, the lifting based architectures claim large amount of frame buffers to store the intermediate LL output and also require complex control path. Andra *et al*., (2002) proposed block based architecture which requires large embedded memory and longer output latency. In combined line-based architecture (Dillen *et al*., 2003), hardware resources are not effectively utilized and it needs to be further optimized. In addition, the DWT and lifting based DWT are suffered by shift invariance and lack of directional selectivity (Mohanty and Meher, 2011) which affects the quality of reproduced image. Kingsbury (2000) and Selesnick *et al* (2005) proposed a DT-DWT to solve the shift variance problem and to improve directional selectivity. Furthermore, a fully shift-invariant lifting based stationary wavelet transform (LSWT) has been proposed by Lee.et.al (2000). On the other hand, both DT-DWT and LSWT needs more lifting hardware and consume more power, which are

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undesirable for high speed and low power image processing applications. Hence, an effective VLSI implementation of modified lifting based dual tree discrete wavelet transform has been proposed in this article to improve the system performance of dual tree wavelet transform by suppressing the frequency components including LH1 and HL1 for reconstruction.

MATERIALS AND METHODS

Lifting scheme:

The fundamental idea behind the lifting scheme is that instead of using scaling functions on the finer level to build a wavelet, it uses an old, simple wavelet and scaling functions on the same level to synthesize a new wavelet. The wavelet filters are implemented using lifting steps such as split, predict, update and normalize. Here, the split phase splits the original signal X(i) into even and odd parts. The prediction step predicts the high pass detailed sub band coefficients and the update stage gives low pass approximation sub band filter coefficients.In9/7 lifting scheme, the implementation of 2D-DWT requires two predictions, two updates and one scaling. A basic 9/7 lifting-based DWT structure is described in Fig.1. The input signal $X(i)$ is decomposed into two parts such as $X(2i)$) and $X(2i+1)$. Then, the first stage of lifting operation is executed as follows (Tinku Acharya and Chaitali Chakrabarti, 2006):

$$p(i)^1 = \alpha\left(X(2i) + X(2i+2)\right) + X(2i+1) \quad (1)$$

$$u(i)^1 = \beta\left(p(i)^1 + p(i-1)^1\right) + X(2i) \quad (2)$$

Where, $p(i)^1$ and $u(i)^1$ represent the first predicted and updated coefficients, α and β are the first level lifting constants. In proposed approach, α = -1.586134342 and β = 0.052980118 are used for first stage lifting process.

The second stage of predict and update of lifting process is given by:

$$p(i)^2 = \gamma\left(u(i)^1 + u(i+1)^1\right) + p(i)^1 \quad (3)$$

$$u(i)^2 = \delta\left(p(i)^2 + p(i-1)^2\right) + u(i)^1 \quad (4)$$

Where, $p(i)^2$ and $u(i)^2$ represent the second lifting predicted and updated coefficients, γ and δ are the second level lifting constants and its typical values are 0.8829110762, 0.4435068522 respectively. The scaling is performed using the normalization parameters K and K^{-1}. In practice, the typical value of normalization factor K is 1.149604398. The normalization is done as follows:

$$u(i) = Ku(i)^2 \quad (5)$$

$$p(i) = p(i)^2 K^{-1} \quad (6)$$

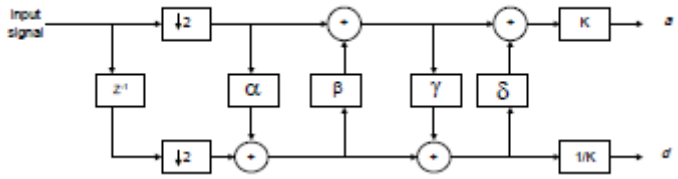

Fig. 1: 9/7 Lifting structure for 9/7 filter.

Lifting based Dual Tree discrete wavelet transform:

In case of DWT, small shifts in the input signal or image can cause significant changes in the distribution of signal/image energy across scales in the DWT coefficients. In addition to that the DWT is not able to discriminate spectral features in different orientations (UfukBal, 2012). In DT-DWT, directional selectivity and shift variance problems are eliminated by processing the same input signal using two different real valued lifting based DWT filters and one of the wavelet filters is an approximate Hilbert transform of the other. In this approach, DWT algorithm is implemented using real filters without complex arithmetic operations. The reverse operation is done at the synthesis part to recover the original image. The analysis and synthesis sections of lifting based dual tree discrete transform (DT-DWT)are illustrated in Fig 2-3.

Modified Lifting based Dual Tree discrete wavelet transform:

The objective of image compression is to exploit the redundant features to reduce the memory storage. As DT-DWT is a redundant transform, it introduces additional redundancy though it achieves good directional selectivity. Hence, the redundancy must be reduced without sacrificing perfect reconstruction and it can be accomplished by simply removing the insignificant complex coefficients (Reeves *et al*., 2002). Though, noise shaping algorithm (NSA) helps to reduce the number of coefficients, it requires more binary data for representation (Reeves *et al*., 2002). Therefore, the modified lifting based dual tree structure has been modified and presented in this article. At the analysis part, the low frequency sub bands (LL1 &LL2) as well as high frequency sub bands (HH1 & HH2) are merged as single sub bands such as LL_m and HH_m respectively and the original image is reconstructed at the synthesis part by using LL_m, HH_m, HL2 and LH2 sub bands. This structure requires less number of lifting hardware and thereby

reducing the power consumption as well as arithmetic computations than the 2D-DWT. Fig.4 demonstrates the analysis section of modified lifting based dual tree structure.

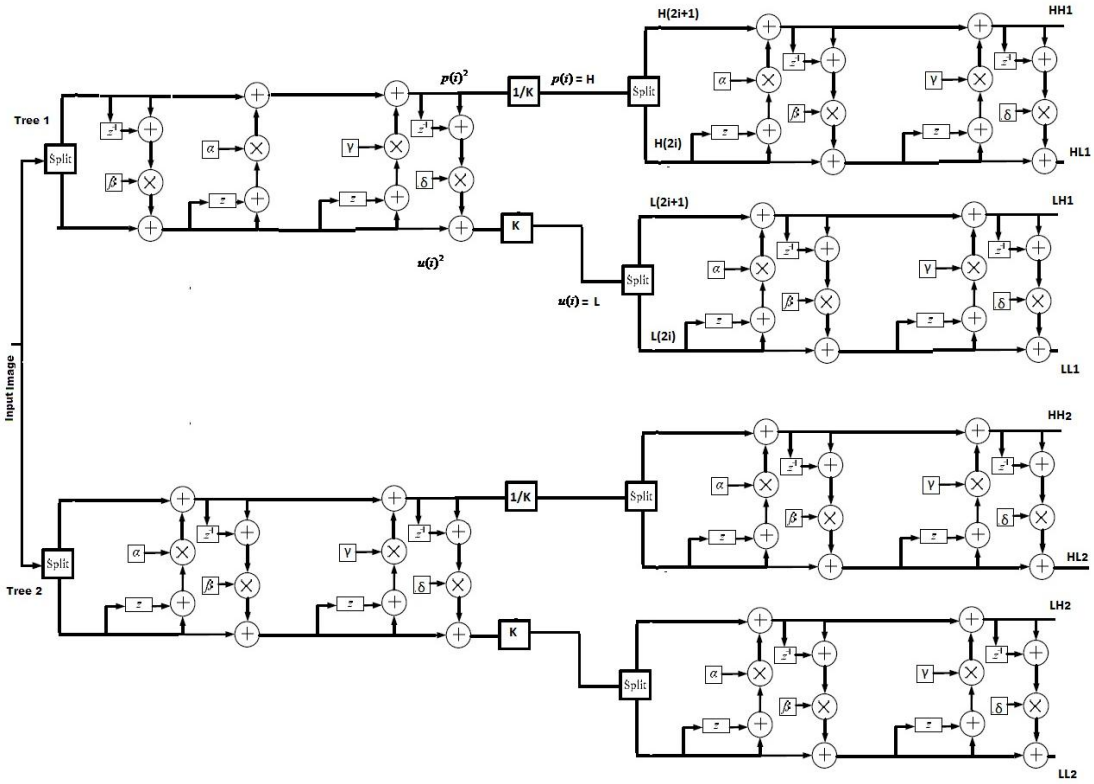

Fig. 2: Analysis Section of Lifting based DT-DWT structure.

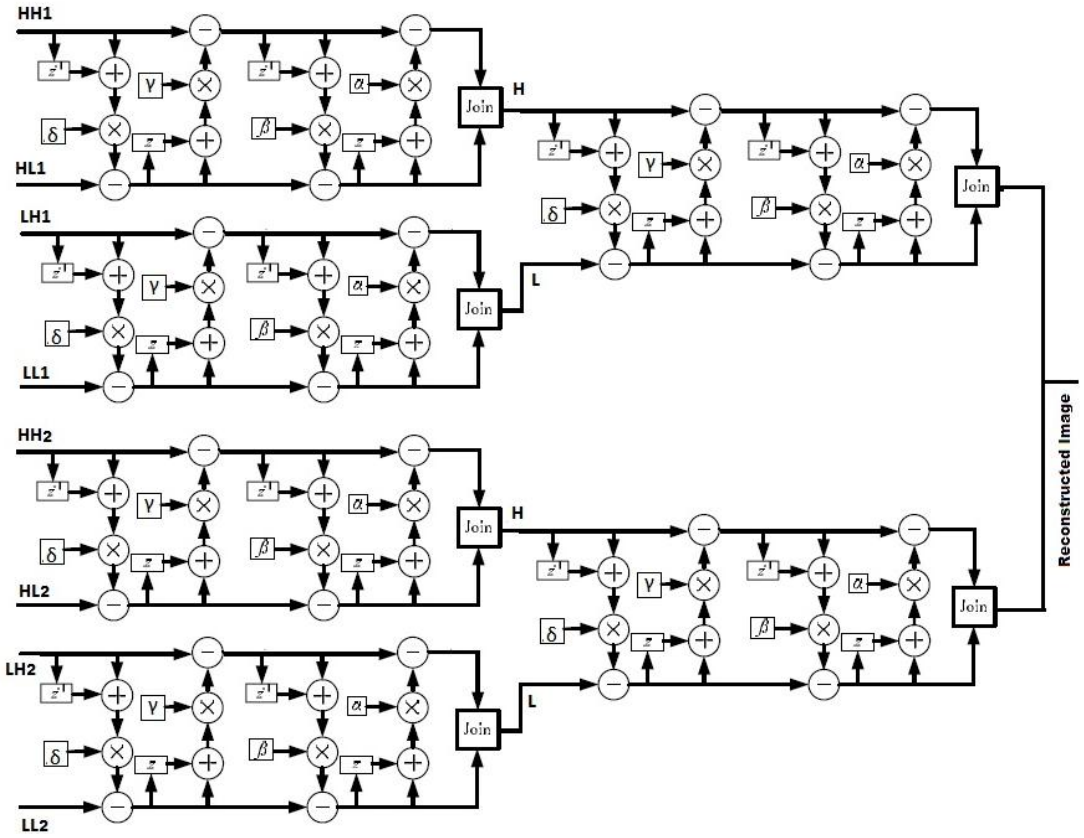

Fig. 3: Synthesis Section of Lifting based DT-DWT structure.

In proposed approach, initially an input image is decomposed up to a desired level by two separable 2D DWT branches using lifting scheme such as, tree 1 and tree2, whose filters are specifically designed to meet the Hilbert pair requirement. At each level of decomposition, six high-pass sub bands as well as two low-pass sub bands are generated. Next, the HH1 and HH2sub bands are linearly combined as HHm. Similarly the low-pass sub bands of each tree are combined as LLm. Finally, the reconstructed image is obtained at the synthesis part by inverting the process performed at the analysis section. Let us assume that ϕ_r and ψ_r be the scaling and wavelet functions of real tree. Let ϕ_i and ψ_i be the scaling and wavelet functions of imaginary tree. The product of φ (.) along the first coordinate and Ψ (.) along the second coordinate correspond to LH sub band. Similarly, wavelets (LH, HL, HH) associated with DWT are given by (Ankit and Bhurane, 2011),

$$\phi(i)\psi(j)=[\phi_r(i)+j\phi_i(i)][\psi_r(j)+j\psi_i(j)]$$
$$=[\phi_r(i)\psi_r(j)-\phi_i(i)\psi_i(j)]+j[\phi_i(i)\psi_r(j)+\phi_r(i)\psi_i(j)] \quad (7)$$

$$\phi(i)\psi^*(j)=[\phi_r(i)+j\phi_i(i)][\psi_r(j)-j\psi_i(j)]$$
$$=[\phi_r(i)\psi_r(j)+\phi_i(i)\psi_i(j)]+j[\phi_i(i)\psi_r(j)-\phi_r(i)\psi_i(j)] \quad (8)$$

$$\phi^*(i)\psi(j)=[\phi_r(i)-j\phi_i(i)][\psi_r(j)+j\psi_i(j)]$$
$$=[\phi_r(i)\psi_r(j)+\phi_i(i)\psi_i(j)]-j[\phi_i(i)\psi_r(j)-\phi_r(i)\psi_i(j)] \quad (9)$$

$$\phi^*(i)\psi^*(j)=[\phi_r(i)-j\phi_i(i)][\psi_r(j)-j\psi_i(j)]$$
$$=[\phi_r(i)\psi_r(j)-\phi_i(i)\psi_i(j)]-j[\phi_i(i)\psi_r(j)+\phi_r(i)\psi_i(j)] \quad (10)$$

$$\psi(i)\phi(j)=[\psi_r(i)+j\psi_i(i)][\phi_r(j)+j\phi_i(j)]$$
$$=[\psi_r(i)\phi_r(j)-\psi_i(i)\phi_i(j)]+j[\psi_r(i)\phi_i(j)+\psi_i(i)\phi_r(j)] \quad (11)$$

$$\psi(i)\phi^*(j)=[\psi_r(i)+j\psi_i(i)][\phi_r(j)-j\phi_i(j)]$$
$$=[\psi_r(i)\phi_r(j)+\psi_i(i)\phi_i(j)]-j[\psi_r(i)\phi_i(j)-\psi_i(i)\phi_r(j)] \quad (12)$$

$$\psi^*(i)\phi(j)=[\psi_r(i)-j\psi_i(i)][\phi_r(j)+j\phi_i(j)]$$
$$=[\psi_r(i)\phi_r(j)+\psi_i(i)\phi_i(j)]+j[\psi_r(i)\phi_i(j)-\psi_i(i)\phi_r(j)] \quad (13)$$

$$\psi^*(i)\phi^*(j)=[\psi_r(i)-j\psi_i(i)][\phi_r(j)-j\phi_i(j)]$$
$$=[\psi_r(i)\phi_r(j)-\psi_i(i)\phi_i(j)]-j[\psi_r(i)\phi_i(j)+\psi_i(i)\phi_r(j)] \quad (14)$$

$$\psi(i)\psi(j)=[\psi_r(i)+j\psi_i(i)][\psi_r(j)+j\psi_i(j)]$$
$$=[\psi_r(i)\psi_r(j)-\psi_i(i)\psi_i(j)]+j[\psi_r(i)\psi_i(i)+\psi_i(i)\psi_r(j)] \quad (15)$$

$$\psi(i)\psi^*(j)=[\psi_r(i)+j\psi_i(i)][\psi_r(j)-j\psi_i(j)]$$
$$=[\psi_r(i)\psi_r(j)+\psi_i(i)\psi_i(j)]-j[\psi_r(i)\psi_i(i)-\psi_i(i)\psi_r(j)] \quad (16)$$

$$\psi^*(i)\psi(j)=[\psi_r(i)-j\psi_i(i)][\psi_r(j)+j\psi_i(j)]$$
$$=[\psi_r(i)\psi_r(j)+\psi_i(i)\psi_i(j)]+j[\psi_r(i)\psi_i(i)-\psi_i(i)\psi_r(j)] \quad (17)$$

$$\psi^*(i)\psi^*(j)=[\psi_r(i)-j\psi_i(i)][\psi_r(j)-j\psi_i(j)]$$
$$=[\psi_r(i)\psi_r(j)-\psi_i(i)\psi_i(j)]-j[\psi_r(i)\psi_i(i)+\psi_i(i)\psi_r(j)] \quad (18)$$

Real-dual tree discrete wavelet transform considers only the real part of the complex wavelets (Ankit and Bhurane, 2011) for the analysis section and it is implemented using two separate lifting based 2DDWT. It produces eightsub bands such as HH2, HL1, LH2, HL2, LH1, HH1, LL1 and LL2 as follows:

$$\psi_{1,1}(i,j)=\phi_r(i)\psi_r(j),\quad \psi_{2,1}(i,j)=\phi_i(i)\psi_i(j)$$
$$\psi_{1,2}(i,j)=\psi_r(i)\phi_r(j),\quad \psi_{2,2}(i,j)=\psi_i(i)\phi_i(j)$$
$$\psi_{1,3}(i,j)=\psi_r(i)\psi_r(j),\quad \psi_{2,3}(i,j)=\psi_i(i)\psi_i(j) \quad (19)$$

Real-dual tree discrete wavelet transform is a redundant and two times expensive. Thus, the proposed structure combines the two high pass bands as well two low pass bands as a single component such as HHm and LLm respectively. Further, it performs the synthesis operation without considering two high pass bands and as a result, the hardware requirement is reduced by a factor of 2 for synthesis operation. The modified synthesis section is shown in Fig.5.

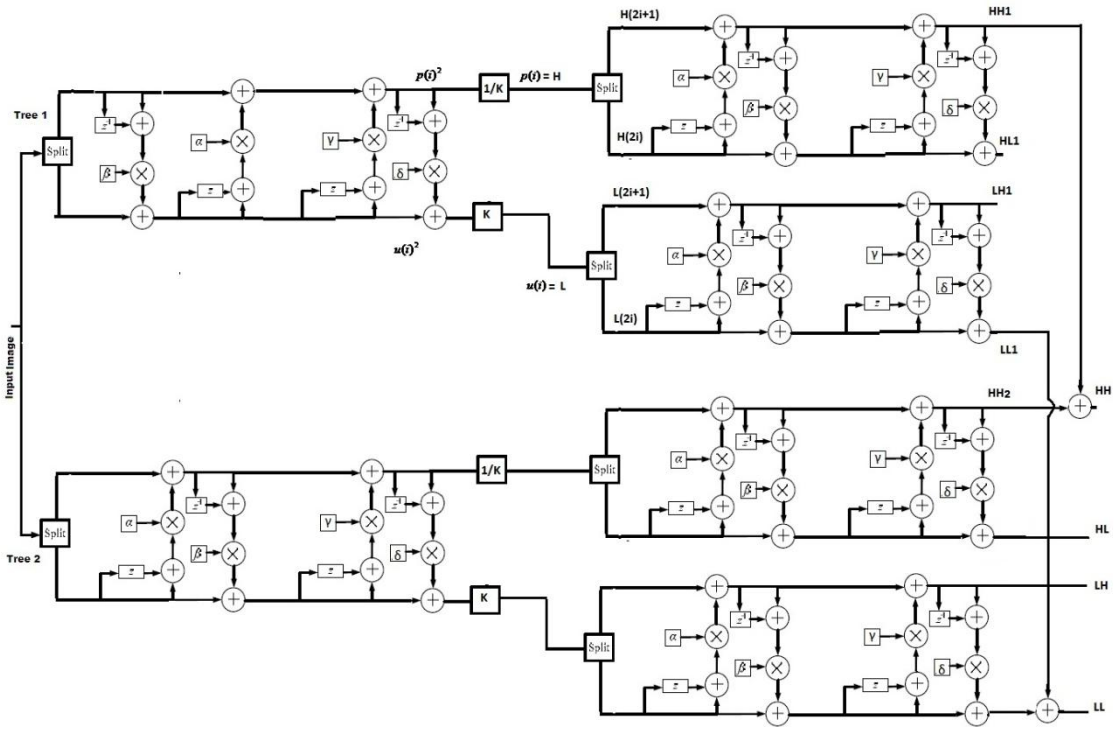

Fig. 4: Analysis section of modified Lifting based dual tree discrete wavelet transform (Proposed).

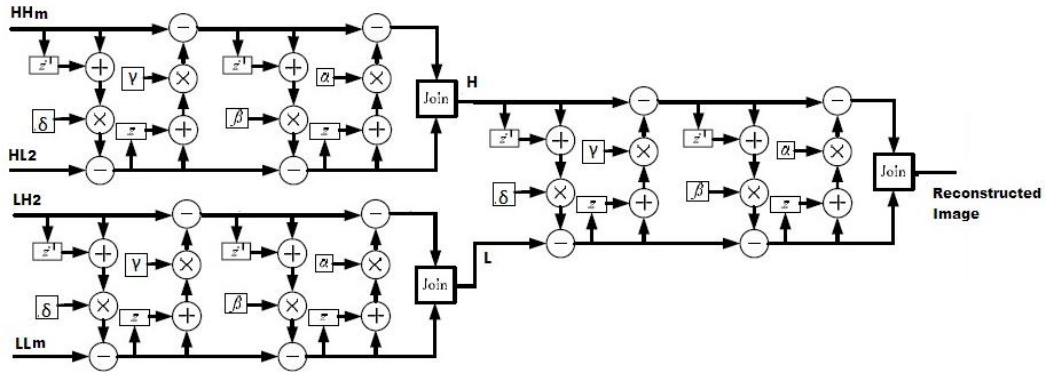

Fig. 5: Synthesis section of modified Lifting based dual tree discrete wavelet transform (Proposed).

Experimental Results and Discussions:

In this section, the performance of proposed approach is qualitatively analyzed and the numerical results of performance metrics are discussed. Experiment was conducted on Intel Pentium® IV 3.0-GHz CPU and 2-GB RAM using Xilinx ISE design suit 14.5 and MATLAB 2010. The proposed approach was tested on test images including "living room.tiff", "house.tiff", "lake.tiff" and "Jet plane.tiff" with image size of 512× 512 and the parameters including Average Absolute Difference (ABSDIFF), Peak Signal to Noise Ratio (PSNR) (Lilian *et al*., 2012 and Amhamed *et al*., 2001), Image Fidelity (IMFID) and Mean Square Error (MSE) (Lilian *et al*., 2012 and Amhamed *et al*., 2001), are considered for performance comparison. These parameters are calculated as follows.

$$ABSDIFF = \frac{1}{MN}\sum_{x=0}^{M-1}\sum_{y=0}^{N-1}\left|o(x,y)-r(x,y)\right| \quad (20)$$

$$PSNR = 20\log_{10}\left(\frac{255^2 MN}{\sum_{x=0}^{M-1}\sum_{y=0}^{N-1}\left|o(x,y)-r(x,y)\right|^2}\right) \quad (21)$$

$$IMFID = \frac{\left(1-\sum_{x=0}^{M-1}\sum_{y=0}^{N-1}\left|o(x,y)-r(x,y)\right|^2\right)}{o(x,y)^2} \quad (22)$$

$$MSE = \frac{1}{MN}\sum_{x=0}^{M-1}\sum_{y=0}^{N-1}\left|o(x,y)-r(x,y)\right|^2 \quad (23)$$

The quality of reconstructed image is analyzed using the above metrics. Peak Signal-to-Noise Ratio (PSNR) measures the noise power with respect to peak signal power and it is often preferred as performance metric for image compression. PSNR must be high for better image quality. The original and reconstructed images of proposed method are

shown in Fig.6. From Fig.6, it can be seen that, the quality of reconstructed image is appreciable and it is an exact replica of the original image. The performance of proposed structure is quantitatively evaluated based on the metrics including ABSDIFF, PSNR, IMFID and MSE and plotted in Fig.7 (a)-(d). The performance of proposed approach is compared with the other existing techniques and it is noted in Table I-V. It is observed that the modified lifting based DT-DWT out performs than other existing techniques. The proposed approach is also simulated using Xilinx ISE design suit 14.5 and the results are reported in Table VI. It is noted that the proposed structure is well suited for low power and high speed image processing applications.

Fig. 6: Original and reconstructed images of proposed approach.

Table I: Performance comparison of ABSDIFF (Absolute difference).

Absolute difference(Absolute difference)				
Images	living room	house	lake	Jetplane
DWT	3.3771	0.4953	3.8376	1.8326
LWT	4.0565	1.0356	4.252	1.9746
DTWT	3.3771	0.7226	3.7916	1.8702
Proposed	2.9106	0.4515	3.6836	1.8051

Table II: Performance comparison of PSNR.

PSNR				
Images	living room	house	lake	Jetplane
DWT	39.8728	38	33.7895	39.9336
LWT	38.3497	44.6125	32.94	39.2967
DTWT	39.8728	47.8538	33.9318	39.6779
Proposed	41.1856	52.1822	34.2946	39.9468

Table III: Comparison of image fidelity.

IMAGE FIDELITY				
Images	living room	house	lake	Jet plane
DWT	-5.48E-04	-0.00012	-0.0013	-0.00022
LWT	-7.79E-04	-0.00012	-0.0016	-0.00028
DTWT	-5.48E-04	-0.00012	-0.0012	-0.00022
Proposed	-4.05E-04	-1.2 E-04	-1.2 E-04	-2.9 E-04

Table IV: Performance comparison of MSE.

MEAN SQUARE ERROR (MSE)				
Images	living room	house	lake	Jet plane
DWT	6.6958	0.4565	25.092	5.5391
LWT	9.5084	2.2344	30.9707	6.55699
DTWT	6.6958	1.0648	24.1367	5.8662
Proposed	4.9494	0.3926	23.0834	5.4534

Table V: Overall performance comparison of proposed approach with existing System.

Method	ABSDIFF	PSNR	IMFID	MSE	Time Complexity (Sec) Analysis section	Time Complexity (Sec) Synthesis Section
DWT	2.38565	37.89898	-5.47E-04	9.44585	0.6543	0.4487

LWT	2.829675	38.79973	-6.95E-04	12.31762	0.6734	0.4580
DTWT	2.44	40.33	-5.22E-04	9.44	1.23	0.8983
Proposed	2.21	41.90	-5.04E-04	8.45	1.28	0.4379

Table VI: Parameter Comparison of Proposed and Existing System.

Parameter	Lifting based DT-DWT		Modified lifting based DT-DWT	
	Analysis	Synthesis	Analysis	Synthesis
Power (mW)	42.41	42.41	42.05	42.14
Delay (nS)	2.265	2.334	1.915	2.334
Registers	187	149	187	108
Memory	48	36	48	20
Buffers	115	111	83	79
FF/Latches	187	149	187	108

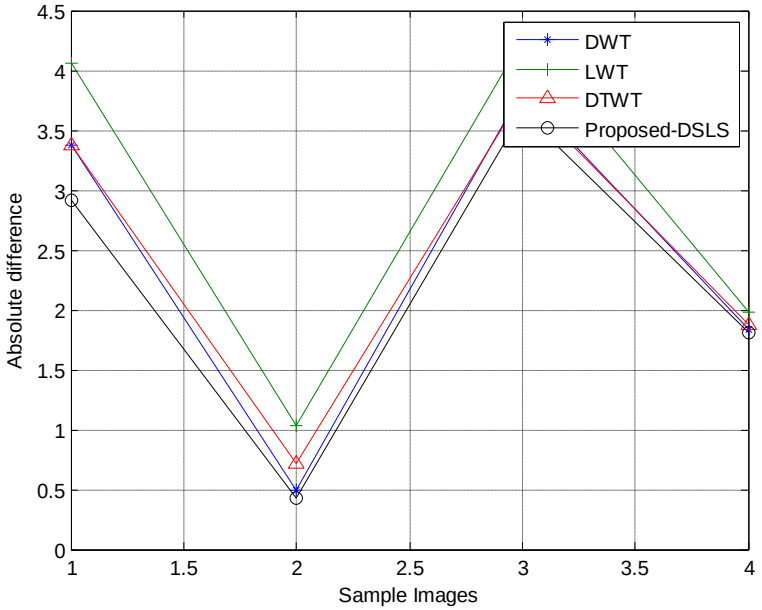

Fig. 7(a): Absolute difference vs. Sample images.

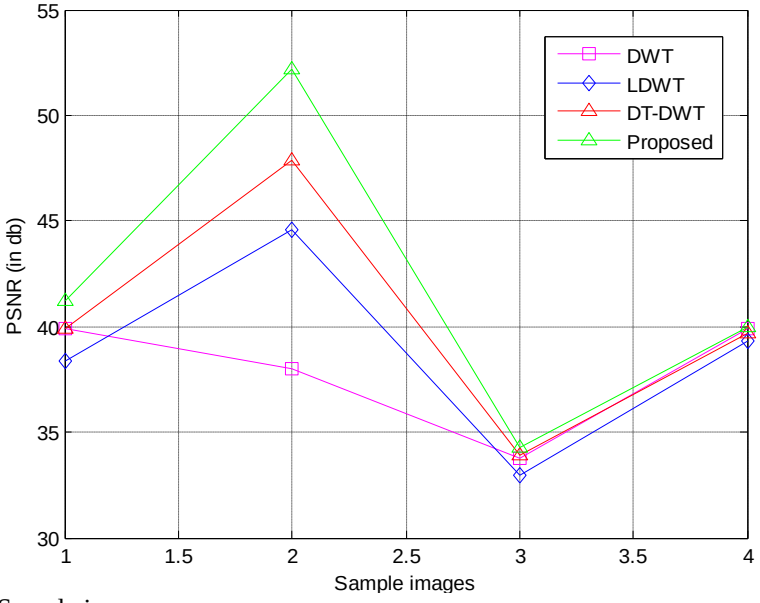

Fig. 7(b): PSNR vs. Sample images.

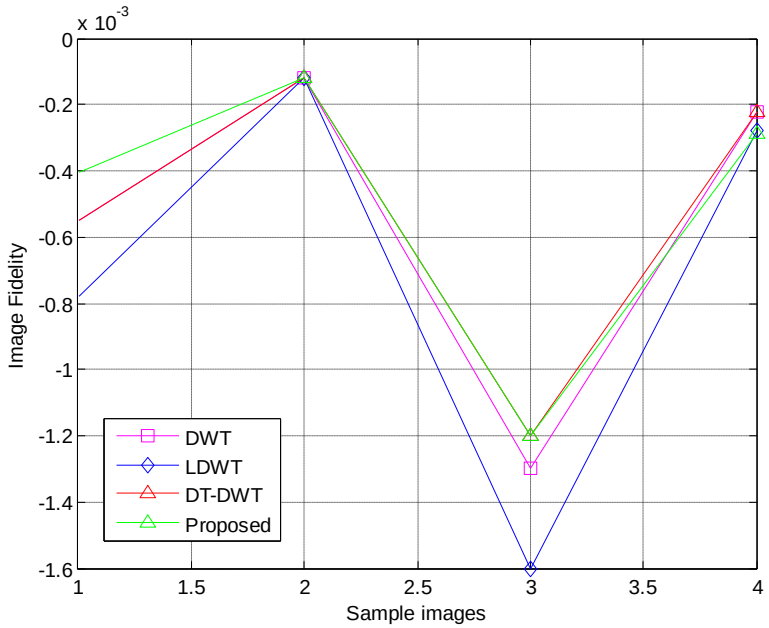

Fig. 7(c): Image Fidelity vs. Sample images.

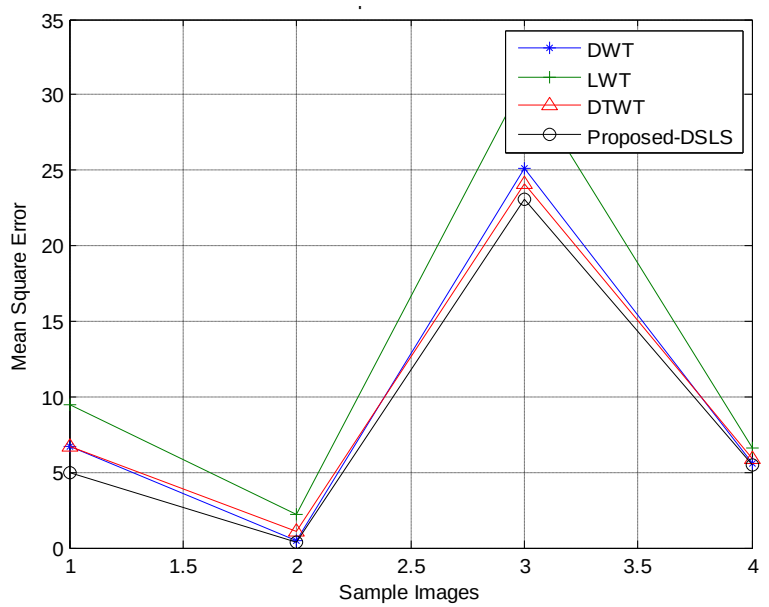

Fig. 7(d): Mean Square Error vs. Sample images.

Fig. 7(a)-(d) Comparison of test results.

Conclusion:

In this paper, a novel modified lifting based DT-DWT has been proposed for low power and high speed image compression applications. An input image is divided into two branches of trees and lifting based DWT using 9/7 filter is applied to each tree at the analysis section. Eight sub bands such asHH2, HL1, LH2, HL2, LH1, HH1, LL1 and LL2 are generated. The high-pass sub bands (HH1 and HH2) and low-pass sub bands (LL1 and LL2) are linearly combined to produce HHm and LLm. The reconstructed image is obtained at the synthesis part without considering two high pass bands (LH1 and HL1) and thus the hardware complexity, power and arithmetic computations are reduced to some extent. Experiment was conducted on four test images using Xilinx ISE design suit 14.5 and MATLAB 2010.The performance was evaluated based on the compression and architectural parameters. Test results show that the modified lifting based DT-DWT is best suited for low power and high speed image processing applications without sacrificing the directional and shift invariant features.

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